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# An efficient algorithm for human face detection and facial feature extraction under different conditions<sup> $\frac{1}{3}$ </sup>

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#### Abstract

In this paper, an efficient algorithm for human face detection and facial feature extraction is devised. Firstly, the location of the face regions is detected using the genetic algorithm and the eigenface technique. The genetic algorithm is applied to search for possible face regions in an image, while the eigenface technique is used to determine the fitness of the regions. As the genetic algorithm is computationally intensive, the searching space is reduced and limited to the eye regions so that the required timing is greatly reduced. Possible face candidates are then further verified by measuring their symmetries and determining the existence of the different facial features. Furthermore, in order to improve the level of detection reliability in our approach, the lighting effect and orientation of the faces are considered and solved. © 2001 Pattern Recognition Society. Published by Elsevier Science Ltd. All rights reserved.

Keywords: Face detection; Facial feature extraction; Genetic algorithm; Eigenface technique

#### 1. Introduction

Digital images and video are becoming more and more important in the multimedia information era. The human face is one of the most important objects in an image or video. Detecting the location of human faces and then extracting the facial features in an image is an important ability with a wide range of applications, such as human face recognition, surveillance systems, human-computer interfacing, video-conferencing, etc. In an automatic face recognition system [1], the first step is to segment the face in an image or video irrespective of whether the background is simple or cluttered. For model-based video coding [2], the synthesis performance is quite dependent on the accuracy of the facial feature extraction process. In other words, a reliable method for detecting the face regions and locating the facial features is indispensable to such applications. This paper presents an efficient method for face detection and facial feature extraction in a cluttered image.

# *1.1. Problems of face detection and facial feature extraction*

In fact, detecting human faces and extracting the facial features in an unconstrained image is a challenging process. It is very difficult to locate the positions of faces in an image accurately. There are several variables that affect the detection performance, including wearing of glasses, different skin coloring, gender, facial hair, and facial expressions. Furthermore, the human face is a three-dimensional (3-D) object, and might be under a distorted perspective and uneven illumination. As a result, a true face may not be detected. Moreover, facial feature extraction is a time-consuming process due to the lack of constraint on the number, location, size, and orientation of faces in an image or a video scene.

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## *1.2. Existing work on face detection and facial feature extraction*

Recently, human face detection algorithms based on color information have been reported [3-5]. The face regions are initially segmented based on the characteristic of skin tone colors. The color signal is usually separated into its luminance and chrominance components in an image or video. Experimental results show that the skin-like regions can be segmented by considering the chrominance components only. Although skin colors differ from person to person, and race to race, they are distributed over a very small area on the chrominance plane. The major difference between the skin tones is intensity. However, human face detection and facial feature extraction in gray-level images may be more difficult because the characteristics of skin tone color are not available. Sung et al. [6] proposed an example-based learning approach for locating vertical frontal views of human faces in complex scenes. A decision-making procedure is trained based on a sequence of "face" and "non-face" examples. Six "face" clusters and six "non-face" clusters are obtained according to 4150 normalized frontal face patterns. The face regions are located by matching the window patterns at different image locations and scales against the distribution-based face model. Yang et al. [7] proposed a hierarchical knowledge-based method consisting of three levels for detecting the face region and then locating facial components in an unknown picture. Mosaic images of different resolutions are used in the two higher levels. Two sets of rules based on the characteristics of a human face region are applied to the mosaic images. At third level, the edges of facial components are extracted for the verification of face candidates. However, the computational requirements of these methods may be too high for some applications, which may be unable to detect and locate a tilted human face reliably.

Extraction of facial features by evaluating the topographic gray-level relief has been introduced [3,8,9]. Since the intensity is low for the facial components, the position of the facial features can be determined by checking the mean gray-level in each row and then in each column. In [9–11], facial feature detection based on the geometrical face model was proposed. The model is constructed based on the relationships among facial organs such as nose, eyes, and mouth. However, these methods can work properly only under well-lit conditions. Therefore, the pre-processing step for reducing the lighting effect is very important for the methods.

In our previous work [12,13], possible face candidates in a gray-level image with a complex background were identified by means of valley features on the human eyes. In this paper, we propose an efficient method for locating the face region and facial features based on the characteristics of eye regions. The face regions are segmented based on a pair of possible eye candidates. The facial features are then extracted from the detected face regions. In order to improve the level of detection reliability, the lighting effect is also considered and alleviated for the possible face regions. This method is tested with the MIT face database and some other complex images. Experimental results show that faces can be detected more reliably and efficiently now compared with our previous work. The details of our approach for face and facial feature detection will be described in the following sections.

### 2. Human face detection using the genetic algorithm and eigenface technique

Our method for detecting and extracting the facial features in a gray-level image is divided into two stages. Firstly, the possible human eye regions are detected by testing all the valley regions in an image. A pair of eye candidates are selected by means of the genetic algorithm [14] to form a possible face candidate. The fitness value of each candidate is measured based on its projection on the eigenfaces [15]. In order to improve the level of detection reliability, each possible face region is normalized for illumination; the shirring effect, when the head is tilted, is also considered as well. After a number of iterations, all the face candidates with a high fitness value are selected for further verification. At this stage, the face symmetry is measured and the existence of the different facial features is verified for each face candidate. The facial features are determined by evaluating the topographic relief of the normalized face regions. The facial features extracted include the eyebrow, the iris, the nostril, and the mouth corner.

Genetic algorithm is an optimization technique that operates on a population of individual solutions. It has been successfully applied for many purposes, such as object recognition [16], human face detection [17,18], facial feature extraction [19], and motion estimation for video coding [20]. In our approach, genetic algorithm is also applied to search for possible facial regions in an image. The first step in locating the face regions in our approach is to select a pair of eye candidates using genetic algorithms. The fitness value for each face candidate is calculated by projecting it onto the eigenfaces space. Since eigenfaces [15] is a successful approach for face recognition, we therefore adopt it as a fitness function.

#### 2.1. Possible eye candidates detection

In our approach, the possible eye regions are located by detecting the valley points in an image. Since the human iris in a gray-level image is of low intensity, a valley exists at an eye region. The valley field  $\Phi_v$ , can be



Fig. 1. Eye candidates detection: (a) original image, (b) possible eye regions, and (c) the good candidates for the detected eye regions.

extracted using morphological operators [21]. The equation for valley field extraction is

$$\Phi_v = f(x, y) \cdot B - f(x, y), \tag{1}$$

where f(x, y) is the image and *B* is the structuring element. The valley image is obtained by performing a closing operation, which is then subtracted by the original image. A pixel at (x, y) is considered as a possible eye candidate if the following criteria are satisfied:

$$f(x, y) < t_l \quad \text{and} \quad \Phi_v(x, y) > t_v, \tag{2}$$

where  $t_l$  and  $t_v$  are thresholds. Fig. 1(a) and (b) shows the original image and its corresponding possible eye regions, respectively. The segmented possible eye regions are then reduced to a point or a number of points by choosing the good candidates in each region. The good eye candidates are those which have large values in the functions, F1(x, y) and F2(x, y). The two functions are defined as follows:

$$F1(x, y) = W_{1,1}\left(\frac{f(x-2, y) + f(x+2, y)}{2} - S_{1,1}(x, y)\right)$$
$$+ W_{1,2}\Phi_{1,1}(x, y), \tag{3}$$

$$F2(x, y) = W_{2,1}\left(\frac{f(x-3, y) + f(x+3, y)}{2} - S_{2,1}(x, y)\right)$$
$$+ W_{2,2}\Phi_{2,1}(x, y),$$

where W's are the weighting factors,  $S_{1,1}(x, y)$  and  $S_{2,1}(x, y)$  are the average gray-level intensities of the region under  $3 \times 3$  and  $5 \times 5$  windows, respectively, and  $\Phi_{1,1}(x, y)$  and  $\Phi_{2,1}(x, y)$  are the average value of the valley field under the  $3 \times 3$  and  $5 \times 5$  windows, respectively. This arrangement allows us to detect the eyes according to different scales. Fig. 1(c) illustrates the good eye candidates for the segmented regions in Fig. 1(b). The locations of the possible eye candidates are stored in



Fig. 2. Structure of a chromosome.

a buffer. In the genetic algorithm, two entries are selected from the buffer to form a possible face candidate. Therefore, the search space is limited to the possible eye candidates, which can then greatly reduce the required runtime.

#### 2.2. Structure of a chromosome

Each solution generated for a problem using the genetic algorithm is called a chromosome or string, which is represented in binary format. In our approach, two components are used to specify a face region in a chromosome. The two components which represent the position of the left eye  $(L_{eye})$  and the right eye  $(R_{eye})$  are the index numbers to the buffer. The structure of the chromosome is illustrated in Fig. 2. The number of bits required to represent the  $L_{eye}$  or  $R_{eye}$  is  $B = \lceil \log_2 N \rceil$ , where N is the total number of detected eye candidates. Thus, the total number of bits in each chromosome is 2B.

Since the size of a human face is proportional to the distance between the two eyes  $(d_{eye})$ , a possible face region which contains the eyebrows, eyes, nose, and mouth can be formed based on this relationship. In our method, a square block is used to represent the detected face region. Fig. 3 shows an example of a selected face region based on the location of an eye pair. The line passing through the centers of the eye pair is called the base line. The extracted possible face regions are subsampled and interpolated to a resolution of  $28 \times 31$ . A low resolution has been proved to be sufficient for face identification. Moreover, the required computation is also reduced due to the fact that fewer pixels need to be manipulated. The relationships between the eye pair, the face size, and the orientation angle  $\theta$  between the base



Fig. 3. The defined geometry of our head model.

line and the x-axis are defined as follows:

$$h_{face} = 1.8d_{eye},\tag{4a}$$

$$h_{eye} = \frac{1}{5} h_{face},\tag{4b}$$

$$w_{eye} = 0.225 h_{face},\tag{4c}$$

$$a = y_2 - y_1,$$

 $b = x_2 - x_1,$ 

$$c = x_2 y_1 - x_1 y_2,$$

$$\theta = \tan^{-1}\left(-\frac{a}{b}\right), \quad -\frac{\pi}{2} \le \theta \le \frac{\pi}{2}.$$
 (4d)

Based on the locations of the eye pairs, a population of possible face regions of different locations, sizes, and orientations can be generated. An initial population of the chromosomes is generated by pairing the possible eye candidates, depicted as white dots in Fig. 1(c). If the total number of detected eye candidates is N, the total number of pairing combinations for the initial chromosomes is N(N - 1)/2. Therefore, members of the initial population are produced by randomly selecting from the N(N - 1)/2 chromosomes.

#### 2.3. Normalization of the possible face regions

The orientation angle of a face candidate can be determined based on the gradient of the eye pair. However, the human face is not a rigid object; it will suffer from a shirring effect if the head is rotated too much, as



Fig. 4. (a) A normal face candidate, and (b) adjusted possible face candidate.



Fig. 5. Shirring angle approximation.

illustrated in Fig. 4. In Fig. 4(a), if the face region is considered to be rectangular, the extracted face will be distorted. However, if the face region is a parallelogram, as shown in Fig. 4(b), the shirring effect is alleviated and a more upright face can be extracted. In our approach, the shirring effect will be compensated when the rotation angle  $\theta > 10^{\circ}$ . In this case, the shirring is estimated to be  $\theta/3$ , which is based on the measurement of over 50 rotated human faces. If the rotation angle is less than  $10^{\circ}$ , the shirring effect may be neglected. If the rotation angle is larger than 10°, two possible face candidates will be generated for a chromosome in the calculation of the fitness values. One candidate uses a rectangular face region, while the other one is adjusted based on the shirring angle of the face. The shirring angle,  $\phi$ , is defined as shown in Fig. 5. This normalization process for the shirring effect is performed using the following transformation:

$$\begin{bmatrix} xr\\ yr \end{bmatrix} = \begin{bmatrix} \tan\phi\sin\theta + \cos\theta & -\tan\phi\cos\theta + \sin\theta\\ -\sec\phi\sin\theta & \sec\phi\cos\theta \end{bmatrix} \times \begin{bmatrix} x\\ y \end{bmatrix},$$
(5)



Fig. 6. (a) Reference face image, (b) original face image with half in shadow, and (c) the histogram normalized face image.



Fig. 7. The crossover process.

Table 1 Parameter settings

Population size	100
Selection probability	0.9
Crossover probability	0.8
Mutation probability	0.08
Chromosome length	2B bits

The value of  $\varepsilon(n)$  is a measure of the distance between the input candidate and the training images. Thus, the fitness function of the possible face region for the *n*th chromosome is defined as

$$f(n) = \frac{1}{\varepsilon(n)}.$$
(7)

From Eq. (7), it follows that a chromosome with a smaller distance will have a larger fitness value. A new population is then generated by means of the genetic operations: selection, crossover, and mutation. A chromosome with a higher fitness value will have a better chance of being chosen for the next generation. In the crossover process, two chromosomes are selected from the mating pool. In our method, the two-point crossover method is employed. Two cutting points are selected randomly within the chromosome for exchanging the contents. The crossover process is illustrated in Fig. 7. Since the probabilities of a chromosome being selected for the crossover and mutation processes are proportional to its computed fitness value, these good offspring will probably be passed on to the next generation. In the order to increase the success rate, the best candidate in one generation can pass directly to the next generation. After a number of iterations, those good candidates will be further verified as to whether they are human faces. The parameter settings used in our approach are shown in Table 1. The extracted good face candidates are then input to the next stage for further verification and facial feature extraction.

### 2.5. Verification of face regions and facial feature extraction

The possible face candidates with a high fitness value are passed on to the second stage. The functions of

where xr and yr denote the coordinates of x and y after compensating for the shirring effect. The derivation of this equation is shown in the appendix.

The detection performance is also affected by the external environment, such as the direction of the lighting source. The uneven lighting conditions make a face become asymmetrical; a true face may not be detected. In order to reduce the lighting effect, the possible face candidates would be normalized by transforming their histograms to the histogram of a reference face image [22] before calculating the fitness value. This can be achieved due to the fact that all human faces have basically the same shape and general illumination properties. The advantage of the histogram normalization is that the size of the reference face image and the input region can be unequal. Thus, it is unnecessary to resample the face candidate to the size of the reference face. Fig. 6 shows an example of the histogram normalization of a face region. After the shirring effect and the histogram normalization processes, the fitness value of the face region will then be computed.

#### 2.4. The fitness function

To determine whether the normalized face candidate is a face or not, the fitness value of the possible face regions is computed by means of the eigenfaces [15]. The eigenfaces are obtained by extracting the principle components from a training-set of pre-processed face images. The training images are also pre-processed by a histogram normalized to reduce the lighting effect. The normalized possible face region is then projected onto the eigenface space in order to calculate the fitness. The fitness function is a measure of the distance between its projection and that of the training-set face images. The distance between the mean adjusted faces  $\Phi$  of the training images and the projection of the mean adjusted input region  $\Phi_f(n)$  for the *n*th chromosome on the face space is calculated by

$$\varepsilon(n) = ||\Phi - \Phi_f(n)||. \tag{6}$$

the second stage are to verify whether the candidates are human faces or not, and to extract the respective facial features in the face region. The verification process is based on the characteristics of the projected face images.

At this stage, the symmetry of a face candidate is measured. As every face region is normalized for the shirring effect and the illumination effect, the difference between the left half and the right half of a face region should be small due to its symmetry. In our method, the size of a face region is normalized to  $28 \times 31$ , and the symmetrical measure is calculated as follows:

$$T_{S} = \frac{1}{434} \sum_{y=0}^{30} \sum_{x=0}^{13} |f(x, y) - f(27 - x, y)|,$$
(8)

where f(x, y) represents a possible face candidate. If the value of  $T_s$  is smaller than the threshold, the face candidate will be selected for further verification. In any overlapping region, the one with the lowest value of  $T_s$  is chosen.

After measuring the symmetry of a face candidate, the existence of the different facial features is also verified. The position of the facial features is determined by analyzing the projection of the normalized face candidate region. The facial feature regions will exhibit a low value on the projection. A normalized face region is divided into three parts; each of which contains the respective facial features. In our method, the y-projection is performed in each part to determine the vertical position of the facial features. The y-projection is the average of the gray-level intensities along each row of pixels in a window. In order to reduce the effect of the background in a face region, only the white windows as shown in Fig. 8 are considered in computing the projections. The two top windows contain the eyebrows and the eyes; the middle window contains the nose; and the bottom window contains the mouth. In each of the windows, the



Fig. 8. Windows for facial feature extraction.

position where the projection value is a minimum is identified. For each of the two top windows, two significant minima will be detected due to the eyebrow and eye, respectively. These minima indicate the vertical position of the eyebrow and the eye. Similarly, the minima in the middle and the bottom windows represent the vertical position of the nostril and the mouth, respectively. The results of the y-direction for the windows in Fig. 8 are shown in Fig. 9. A valid minimum is identified by measuring the difference between the minimum and its neighboring maximum. If the vertical position of any of the facial features cannot be found, the face candidate is then declared as a non-facial image, and is rejected from the x-projection process.

Having obtained the vertical position of the respective facial features, the horizontal position of the facial features is then determined by the x-projection. The x-projection is computed by averaging the gray-level intensities on each column in a window. The position of the eyes can be estimated by performing an x-projection around their vertical position and identifying the location of the two minimal points of the projection. For the eyebrows, sudden changes in the x-projection values signify the end points of the eyebrows. To detect the horizontal position of a nostril in the middle window, two significant minima and a maximum between the two minima will be obtained. The first minimum represents the horizontal position of the left nostril, while the second minimum represents the right nostril. Fig. 10(a) shows the x-projection for determining the nostrils. For the bottom window, the mouth corner can be detected based on two assumptions; the mouth corners are close to the horizontal position of the corresponding iris and the gray-level intensity changes significantly at the mouth corner. Fig. 10(b) illustrates the x-projection and the determination of the detected mouth corners. The detection result for the respective facial features is shown in Fig. 11. Similarly, if any horizontal position of the facial features cannot be located, the candidate is assumed to be a non-facial image. Otherwise, a true face region is declared, as are the different facial features being located.

#### 3. Experimental results

In our approach, if the fitness value of the chromosome is greater than the threshold, it is assumed to be a possible face candidate. These possible face candidates will pass into the second stage for further verification. In the second stage, the symmetry of a face candidate will be calculated. If the difference between the left- and righthalf regions of the candidate is greater than the threshold, it is declared a non-facial image. Otherwise, the projection processes will be applied to detect the respective facial features. If the projection results of the face



Fig. 9. The y-projection results of (a) eye region, (b) nose region, and (c) the mouth region.

candidate do not fulfill the defined rules for facial features, the face candidate will also be declared a non-facial image.

The detection performance of our method is tested using the face database from MIT and some images with a number of faces. In the experiment, the training set images are different from the test images. Table 2 shows both the hit and miss rates of our method of face detection under different conditions. This approach can achieve an overall hit rate of 100% without head tilt and under head-on lighting. When the heads tilt to the left or right, the hit rate is 95.3%. When the light source to the faces is  $45^{\circ}$ , the hit rates for the upright and tilted faces are 87.5 and 82.8%, respectively. When the lighting is  $90^{\circ}$ , the hit rate for the upright face is 93.75% and the hit rate for the tilted face is 81.25%. The experiment shows that the hit rates for a tilted face after performing shirring normalization have a great improvement over our previous work on face detection.

The hit rates for facial feature detection are tabulated in Table 3. In this part, only those faces detected successfully are considered. The reasons for the failure in detecting the facial features can be summarized as follows: facial images with glasses may affect the determination of



Fig. 10. The x-projection results of (a) nose region, and (b) the mouth region.



Fig. 11. An example of facial feature extraction by analyzing the projection of normalized face region.

the eyebrows; nostril detection is highly affected by the lighting conditions; and a moustache in a facial image covers the mouth corners. Fig. 12 shows the detection results under different lighting conditions and different angles of rotation, while Fig. 13 illustrates some errors in locating the facial features.

Our method is extended to the detection of multiple faces in an image. A user may choose to make either a single-face or a multiple-faces detection. The respective processes for detecting a single face and multiple faces are very similar. The major difference is in the threshold setting in stage one: the threshold value for single-face detection is greater than that for multiple-faces detection. This means that more face candidates may pass into the next stage in multiple-faces detection. Thus, false alarms will happen in this case. We have tested 20 images with multiple-faces (2–3 faces in each of the images). The total number of false alarms is 6, while the hit rate is 92%. The experiments were performed on a Pentium II 400 MHz computer. The average processing time for locating faces and the facial features in a picture of size  $128 \times 120$  is about 2.18 s. In conclusion, this method outperforms those used in our previous work.

#### 4. Conclusion

In this paper, we have proposed a more reliable face detection approach based on the genetic algorithm and the eigenface technique. Firstly, possible eye candidates are obtained by detecting the valley points. Based on a pair of eye candidates, possible face regions are generated by means of the genetic algorithm. Each of the possible face candidates is normalized by approximating the shirring angle due to head movement. Furthermore, the lighting effect is reduced by transforming their histograms into the histogram of a reference face image. The fitness value of a face candidate is calculated by projecting it onto the eigenfaces. Selected face candidates are then further verified by measuring their symmetries and determining the existence of the different facial features. The advantages of our approach are that a tilted human face can still be detected robustly even if the face is shirred, under shadow, of a different scale, under bad lighting conditions, and is wearing glasses. In conclusion, this method can achieve a high-performance level in detecting human faces and extracting facial features in complex and simple backgrounds.

#### Appendix

A face region under shirring effect is illustrated in Fig. 14(a), where  $\theta$  and  $\phi$  are the angle of rotation and

	Lighting	Head on		<b>15</b> °		000	
				43		90	
	Head tilt	No	Tilt	No	Tilt	No	Tilt
Full scale	Hit Miss	16 0	30 2	15 1	26 6	16 0	26 6
Medium scale	Hit Miss	16 0	31 1	13 3	27 5	14 2	26 6

Table 2Experimental results for face detection

#### Table 3

Experimental results for the facial feature extraction

	Lighting	Head on		45°	45°		90°	
	Head tilt	No	Tilt	No	Tilt	No	Tilt	
Full scale	Hit rate of first part (eyebrow and iris)	$\frac{16}{16}$	$\frac{30}{30}$	$\frac{15}{15}$	$\frac{25}{26}$	$\frac{16}{16}$	$\frac{25}{26}$	
	Hit rate of middle part (nostril)	$\frac{16}{16}$	$\frac{29}{30}$	$\frac{15}{15}$	$\frac{24}{26}$	$\frac{15}{16}$	$\frac{23}{26}$	
	Hit rate of bottom part (mouth corner)	$\frac{15}{16}$	$\frac{28}{30}$	$\frac{14}{15}$	$\frac{24}{26}$	$\frac{14}{16}$	$\frac{22}{26}$	
Medium scale	Hit rate of first region (eyebrow and iris)	$\frac{16}{16}$	$\frac{31}{31}$	$\frac{13}{13}$	$\frac{26}{27}$	$\frac{13}{14}$	$\frac{24}{26}$	
	Hit rate of middle part (nostril)	$\frac{16}{16}$	$\frac{31}{31}$	$\frac{12}{13}$	$\frac{26}{27}$	$\frac{13}{14}$	$\frac{23}{26}$	
	Hit rate of bottom part (mouth corner)	$\frac{15}{16}$	$\frac{29}{31}$	$\frac{11}{13}$	$\frac{24}{27}$	$\frac{12}{14}$	$\frac{22}{26}$	

the shirring angle, respectively. Rotating the region about the point O by an angle  $\theta$ , the rotation transformation is as follows:

$$\begin{bmatrix} x'\\ y' \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta\\ -\sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} x\\ y \end{bmatrix}.$$
 (A1)

The rotated region is illustrated in Fig. 14(b). Let pt1 be the point before normalization and pt2 be the point after shirring normalization, then

$$\frac{x' - x''}{y'} = \tan \phi \Rightarrow x'' = x' - y' \tan \phi,$$
$$(y'')^2 = l^2 = y'^2 + (x' - x'')^2,$$

$$(y'')^2 = (y')^2 + (x' - (x' - y' \tan \phi))^2,$$

$$\Rightarrow y'' = y' \sec \phi$$

$$\begin{bmatrix} x'' \\ y'' \end{bmatrix} = \begin{bmatrix} 1 & -\tan\phi \\ 0 & \sec\phi \end{bmatrix} \begin{bmatrix} x' \\ y' \end{bmatrix}.$$

From Eq. (A1), we have

$$\begin{bmatrix} x''\\y'' \end{bmatrix} = \begin{bmatrix} 1 & -\tan\phi\\0 & \sec\phi \end{bmatrix} \begin{bmatrix} \cos\theta & \sin\theta\\-\sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} x\\y \end{bmatrix},$$
$$\begin{bmatrix} x''\\y'' \end{bmatrix} = \begin{bmatrix} \cos\theta + \tan\phi\sin\theta & \sin\theta - \tan\phi\cos\theta\\-\sin\theta\sec\phi & \cos\theta\sec\phi \end{bmatrix} \begin{bmatrix} x\\y \end{bmatrix}.$$



Fig. 12. (a) Experimental results under head-on lighting, (b) experimental results when the lighting is  $45^{\circ}$ , (c) experimental results when the lighting is  $90^{\circ}$ , and (d) some more experimental results.



Fig. 13. Error in facial feature extraction.



Fig. 14. (a) A region under shirring effect, and (b) the rotated region.

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